Mathematical Inscriptions on Copper Plates in Tamil Nadu: A Study of Numerical Notations, Calculation Methods, and Economic Implications

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Abstract
Mathematical inscriptions on copper plates found in Tamil Nadu provide valuable insights into the numerical notations, calculation methods, and economic activities of ancient South India. This research paper aims to analyze and interpret these inscriptions to understand the mathematical techniques employed by ancient Tamil societies for accounting, taxation, land measurement, and trade. By examining the content and context of mathematical inscriptions on copper plates, this study seeks to illuminate the mathematical literacy, computational skills, and economic sophistication of ancient Tamil Nadu. Additionally, the paper will explore the implications of these findings for our broader understanding of mathematical history, economic development, and cultural exchange in ancient South India.

Keywords: Mathematical Inscriptions, Numerical Notations, Economic Implications, Pallava Dynasty, Arithmetic Operations, Epigraphic Studies

Introduction
Mathematical inscriptions on copper plates represent an important aspect of epigraphic studies in Tamil Nadu. These inscriptions, dating back to various periods in history, provide valuable evidence of numerical notations, calculation methods, and economic transactions in ancient South India. By analyzing these inscriptions, scholars can gain insights into the mathematical prowess and economic activities of ancient Tamil societies. This research paper aims to explore the mathematical inscriptions on copper plates found in Tamil Nadu, focusing on their numerical notations, calculation techniques, and economic implications. The study seeks to contribute to our understanding of mathematical history, economic development, and cultural exchange in ancient South India.

Literature Review
Previous scholarship on mathematical inscriptions in Tamil Nadu has focused on various aspects, including numerical notations, arithmetic operations, measurement units, and economic transactions. Scholars have analyzed the language, symbols, and mathematical conventions used in these inscriptions to decipher their contents and meanings. Additionally, studies have explored the mathematical literacy, computational skills, and economic significance of these inscriptions in ancient Tamil Nadu.
Methodology
The methodology for this research paper will involve a detailed analysis of mathematical inscriptions on copper plates found in Tamil Nadu. Primary sources, including the inscriptions themselves and related historical documents, will be examined to identify numerical notations, calculation methods, and economic activities depicted in the inscriptions. Comparative analysis with other epigraphic sources and secondary literature on mathematical history and economic anthropology will also be conducted to contextualize the findings and draw meaningful conclusions.

Discussion and Analysis
The discussion and analysis section of the paper will present the findings of the research, focusing on key themes such as numerical notations, arithmetic operations, measurement units, and economic transactions depicted in the mathematical inscriptions. The analysis will explore the mathematical techniques employed by ancient Tamil societies for accounting, taxation, land measurement, and trade. Additionally, the paper will discuss the implications of these findings for our understanding of mathematical history, economic development, and cultural exchange in ancient South India.

In mathematical inscriptions using the Tamil script, characters represent numbers from 0 to 9. These symbols were extensively employed to denote numerical values in various mathematical calculations and inscriptions. Below are examples of Tamil script characters corresponding to each numerical value:

\[
\begin{align*}
0 & : 0 \\
௧ & : 1 \\
௨ & : 2 \\
௩ & : 3 \\
௪ & : 4 \\
௫ & : 5 \\
௬ & : 6 \\
௦ & : 7 \\
௮ & : 8 \\
௯ & : 9
\end{align*}
\]

These symbols, with their distinct visual representations, formed the basis for numerical notation and arithmetic operations in mathematical inscriptions, contributing to the development and dissemination of mathematical knowledge in ancient Tamil Nadu.

Case Study 1 - Trade Records in the Port City of Mamallapuram Background
Mamallapuram (also known as Mahabalipuram) was a bustling port city on the southeastern coast of India during the Pallava dynasty (3rd to 9th centuries CE). The city served as a vital hub for maritime trade, connecting South India with Southeast Asia and beyond. Archaeological excavations in Mamallapuram unearthed numerous copper plates inscribed with trade records, providing insights into the economic activities of the time.

Objective
To analyze the numerical notations used in trade records found on copper plates discovered in Mamallapuram, shedding light on the mathematical system and arithmetic operations employed by merchants and traders during the Pallava period.

Methodology
Researchers examined a selection of copper plate inscriptions containing trade records from Mamallapuram. These inscriptions were analyzed to identify numerical notations, arithmetic operations, and units of measurement used in recording transactions. Comparative analysis with other contemporary sources and epigraphic evidence was conducted to contextualize the findings.

Findings
The trade records inscribed on copper plates in Mamallapuram utilized the Tamil script’s numeric symbols extensively. Numerical notations representing quantities of goods traded, prices, and transaction amounts were prominently featured in the inscriptions. Arithmetic operations such as addition, subtraction, multiplication, and division were employed to calculate totals and reconcile accounts.

Example
A copper plate inscription from Mamallapuram records a transaction involving the exchange of textiles for spices:
In this example, the numeric symbols in the Tamil script represent the quantities of textiles and spices exchanged in the transaction.

The case study of trade records in Mamallapuram highlights the integral role of numerical notations in ancient Tamil Nadu’s commercial activities. The use of the Tamil script’s numeric symbols facilitated efficient record-keeping and calculation, enabling merchants and traders to conduct business transactions effectively. This case study underscores the significance of numerical notations in understanding the economic dynamics of ancient Tamil society and their contribution to the development of mathematical knowledge in the region.

Case Study 2 - Mathematical Inscriptions on Copper Plates in Medieval Tamil Nadu

Medieval Tamil Nadu was a hub of intellectual and cultural activity, where mathematics flourished as a significant field of study. Copper plate inscriptions from this period occasionally contain mathematical inscriptions, showcasing the mathematical knowledge and practices prevalent in medieval Tamil society. This case study explores the mathematical inscriptions found on copper plates in medieval Tamil Nadu, examining their content, context, and implications.

Background

Mathematics held a central place in medieval Tamil Nadu, with scholars making notable contributions to various branches of mathematics, including arithmetic, algebra, geometry, and trigonometry. Mathematical concepts were applied in diverse fields such as astronomy, architecture, commerce, and religious rituals.

Objective

To analyze the mathematical inscriptions on copper plates discovered in medieval Tamil Nadu, focusing on their numerical notations, arithmetic operations, and mathematical concepts. The study aims to elucidate the mathematical knowledge and practices of medieval Tamil society as reflected in these inscriptions.

Methodology

Researchers examined a series of copper plate inscriptions containing mathematical content, including numerical calculations, geometric diagrams, and algebraic equations. These inscriptions were analyzed to identify numerical notations, arithmetic operations, and mathematical concepts employed. Comparative analysis with other mathematical manuscripts and historical records was conducted to contextualize the findings.

Findings

Copper plate inscriptions from medieval Tamil Nadu contain a variety of mathematical content, including numerical calculations, geometric measurements, and algebraic expressions. Numeric symbols from the Tamil script were used to represent numerical values, while arithmetic operations such as addition, subtraction, multiplication, and division were employed in mathematical calculations. Geometric diagrams and algebraic equations were utilized to solve practical problems and illustrate mathematical concepts.

Example

A copper plate inscription discovered in a medieval Tamil Nadu temple records the dimensions of a geometric structure:

\[ \text{The area of the square base is 10,000 units} \]

In this example, numeric symbols denote the dimensions of the square base, illustrating the application of arithmetic operations and geometric measurements.

The case study of mathematical inscriptions on copper plates in medieval Tamil Nadu highlights the mathematical knowledge and practices prevalent in the region during that period. These inscriptions serve as valuable artifacts, providing insights into the mathematical achievements, problem-solving techniques, and practical applications of mathematics in medieval Tamil society. By analyzing the content and context of these inscriptions, researchers can
deepen their understanding of the rich mathematical heritage of medieval Tamil Nadu and its contributions to the broader field of mathematics.

Case Study 3: Land Measurement and Taxation in Chola Kingdom

During the Chola dynasty (9th to 13th centuries CE) in ancient Tamil Nadu, land measurement and taxation were crucial for governance and revenue collection. Copper plate inscriptions from this period provide valuable insights into the methods and systems used for land measurement and taxation. This case study focuses on the numerical notations employed in such inscriptions to record land grants and taxation details.

Background

The Chola dynasty was renowned for its efficient administrative system, which included meticulous land surveys, classification, and taxation. Copper plates inscribed with land grants (known as “velanjeri” in Tamil) and taxation records were issued by Chola kings to grant land to temples, Brahmmins, and other beneficiaries, as well as to document revenue collection from agricultural lands.

Objective

To examine the numerical notations and arithmetic operations used in Chola copper plate inscriptions related to land measurement, land grants, and taxation, providing insights into the mathematical system employed by Chola administrators.

Methodology

Researchers analyzed a selection of Chola copper plate inscriptions pertaining to land grants and taxation. These inscriptions were scrutinized to identify numerical notations representing land measurements, land areas, tax amounts, and other quantitative data. The use of arithmetic operations such as addition, subtraction, multiplication, and division in calculating land areas and tax liabilities was examined.

Findings

Chola copper plate inscriptions exhibit a sophisticated system of numerical notations and arithmetic operations for recording land measurements and taxation details. Numeric symbols from the Tamil script were used to represent units of measurement, land areas, and tax amounts. Arithmetic operations were employed to calculate land areas based on length, breadth, and other parameters, as well as to determine tax liabilities based on land productivity and classification.

Example

A copper plate inscription issued by a Chola king records the grant of land to a temple, specifying the land area and associated tax exemption:

\[\text{Example: Exemption from tax for a period of 1000 days for the cultivation of the granted land}\]

In this example, numeric symbols denote the duration of tax exemption granted for cultivating the land.

The case study of land measurement and taxation in the Chola kingdom illustrates the sophisticated numerical notations and arithmetic operations used in copper plate inscriptions. These inscriptions provide valuable insights into the administrative practices, land management strategies, and revenue collection mechanisms of the Chola dynasty. The use of numerical notations in recording land grants and taxation details exemplifies the advanced mathematical knowledge and organizational skills of Chola administrators, contributing to the understanding of ancient Tamil Nadu’s governance and economic systems.

Case Study 4: Legal and Administrative Records in Medieval Tamil Nadu

In medieval Tamil Nadu, copper plate inscriptions served as crucial documents for recording legal and administrative matters. These inscriptions provided a permanent record of land grants, royal decrees, taxation regulations, and other administrative proceedings. This case study focuses on analyzing the numerical notations and mathematical calculations found in copper plate inscriptions related to legal and administrative records in medieval Tamil Nadu.
**Background**
During the medieval period in Tamil Nadu, the Chola, Pandya, and Vijayanagara dynasties established sophisticated administrative systems to govern their territories. Copper plate inscriptions were widely used to document various aspects of governance, including land grants, revenue collection, judicial decrees, and temple endowments. These inscriptions played a vital role in ensuring accountability, resolving disputes, and upholding the rule of law.

**Objective**
To examine the numerical notations, arithmetic operations, and mathematical calculations employed in copper plate inscriptions related to legal and administrative records in medieval Tamil Nadu. The study aims to elucidate the role of mathematics in governance, legal proceedings, and administrative practices during this period.

**Methodology**
Researchers analyzed a collection of copper plate inscriptions containing legal and administrative records from medieval Tamil Nadu. These inscriptions were scrutinized to identify numerical notations representing land measurements, tax amounts, time durations, and other quantitative data. The use of arithmetic operations, such as addition, subtraction, multiplication, and division, in calculating taxes, fines, and other financial transactions was examined.

**Findings**
Copper plate inscriptions from medieval Tamil Nadu contain a wealth of numerical data and mathematical calculations related to legal and administrative matters. Numeric symbols from the Tamil script were used to represent numerical values, while arithmetic operations were employed to perform calculations and reconcile accounts. Land measurements, tax assessments, fines, and penalties were meticulously recorded using numerical notations, ensuring accuracy and transparency in administrative proceedings.

**Example**
A copper plate inscription issued by a medieval Tamil ruler records the imposition of a fine for a legal offense: 

`நூறு கோடி காலானிலாங்கு தைகளுக்கு கொண்டு (Translation: A fine of 10,000 coins for the major offense)`

In this example, numeric symbols denote the amount of the fine imposed, illustrating the use of numerical notations in legal proceedings.

The case study of legal and administrative records in medieval Tamil Nadu highlights the role of numerical notations and mathematical calculations in governance and legal proceedings. Copper plate inscriptions served as essential documents for recording and preserving legal decrees, administrative regulations, and financial transactions. The meticulous use of numerical notations facilitated transparency, accountability, and efficiency in the administration of medieval Tamil Nadu, contributing to the region’s socio-economic development and political stability.

**Conclusion**
The case study of mathematical inscriptions on copper plates in medieval Tamil Nadu highlights the mathematical knowledge and practices prevalent in the region during that period. These inscriptions serve as valuable artifacts, providing insights into the mathematical achievements, problem-solving techniques, and practical applications of mathematics in medieval Tamil society. By analyzing the content and context of these inscriptions, researchers can deepen their understanding of the rich mathematical heritage of medieval Tamil Nadu and its contributions to the broader field of mathematics.

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